

# The SAT Solver KW

BY JOHAN ALFREDSSON, OEPIR CONSULTING

johan@oepir.com

## Introduction

KW is a propositional satisfiability solver. The aim when creating it has been to build a flexible SAT framework that can easily be extended in several directions. Therefore, the architecture is extremely modular and in the trade-off between speed and generality, the latter has almost always been favoured. At the heart of the KW solution process is a strategy selection mechanism [1] that time-slices different strategies to simplify and solve the problem instances. KW supports incremental problem solving and proof generation.

## Strategies

KW is parametrized over which strategies to use to try to solve a SAT instance. Currently, the following strategies are available:

**DPLL.** The implementation features most modern extensions like 1-UIP conflict generation [2], conflict clause minimization [3], watched literals [4], efficient VSIDS heuristics and rapid restarts [5].

**Intersection.** By branching on both a literal and its complement and recording the similarities between these propagation results, information about literal values can be propagated which simplifies the problem instance. Further details exist in [6].

**Strongly connected components.** Finding the strongly connected components of the binary implication graph, equivalent literal information is extracted. By selecting representatives for equivalence classes of literals, the clause database may be simplified after a representative literals normalization. For further information, see [7].

**Variable elimination.** By performing all possible resolutions and adding those to the clause database, a variable can be eliminated from the problem instance. To avoid extensive problem growth, only variables which do not generate a big increase in memory usage are eliminated [8].

**Subsumption.** A clause for which there is another shorter clause in the clause database containing only literals from the first clause is redundant. This strategy finds and removes such redundant clauses [9]. It also finds similar redundancies after one resolution step.

**Automatic.** This is a meta-strategy that select the next strategy to run from a set of allowed strategies.

## Circuit support

KW supports solving circuit SAT problems formulated in the AIGER [10] format. Currently, only a simple translation from AIGER to CNF is done using a naive Tseitin transformation [11] after which the regular CNF instance solving takes over.

## Future work

KW still lacks many bells and whistles. The primary road ahead consists of adding more strategies to complement the existing ones. Two more strategies are in development and yet three more are planned. Furthermore, the idea is to improve the capabilities of solving circuit problems. There is also on-going work to streamline the KW API to suit particular higher-level user applications.

## References

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